Jena NA Summer School 2025

Tensors and numerical multilinear algebra

Some references for further reading (highly incomplete)

Overview articles

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Low-rank matrix optimization (lecture 1)

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Tensors and basic approximation algorithms (lectures 2 & 3)

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